Funding Valuation Adjustment

Funding Valuation Adjustment Introduction

◆ Funding valuation adjustment is introduced to capture the incremental costs of funding uncollateralized derivatives.

◆ Funding valuation adjustment is the difference between the rate paid for the collateral to the bank's treasury and rate paid by the clearinghouse.

◆ Funding valuation adjustment can be thought of as a hedging cost or benefit arising from the mismatch between an uncollateralized derivative and a collateralized hedge in the interdealer market.

Master Agreement

◆ Master agreement is a document agreed between two parties, which applies to all transactions between them.

◆ Close out and netting agreement is part of the Master Agreement.

◆ If two trades can be netted, the credit exposure is
$$E(t) = max(V_1(t) + V_2(t), 0)$$

◆ If two trade cannot be netted (called non-netting), the credit exposure is
$$E(t) = max(V_1(t), 0) + max(V_2(t), 0)$$

CSA Agreement

◆ Credit Support Annex (CSA) or Margin Agreement or Collateral Agreement is a legal document that regulates collateral posting.

◆ Trades under a CSA should be also under a netting agreement, but not vice verse.

◆ It defines a variety of terms related to collateral posting.

- ◆ Threshold
- ◆ Minimum transfer amount (MTA)
- ◆ Independent amount (or initial margin or haircut)

Risk Neutral Simulation: Interest Rate and FX

◆ Recommended 1-factor model: Hull-White

$$dr_t = (\theta_t - \alpha r_t)dt + \sigma_t dW_t$$

◆ Recommended multi-factor model: 2-factor Hull-White or Libor Market Model (LMM)

◆ All curve simulations should be brought into a common measure.

    ◆ Simulate interest rate curves in different currencies.

    ◆ Change measure from the risk neutral measure of a quoted currency to the risk neutral measure of the base currency.

◆ Forward FX rate can be derived using interest rate parity

$$F = S_0 exp(r_s - r_q)t$$

Risk Neutral Simulation: Equity Price

◆ Geometric Brownian Motion (GBM)

$$\frac{dr}{r} = \mu dt + \sigma dw$$

◆ Pros

  ◆ Simple
  ◆ Non-negative stock price

◆ Cons

  ◆ Simulated values could be extremely large for a longer horizon.

Risk Neutral Simulation: Commodity Price

◆ Simulate commodity spot, future and forward prices as well as pipeline spreads

◆ Two factor model

$$\log(S_t) = q_t + \mathcal{X}_t + \mathcal{Y}_t$$
$$d\mathcal{X}_t = (\alpha_1 - \gamma_1 \mathcal{X}_t)dt + \sigma_1 dW_t^1$$
$$d\mathcal{Y}_t = (\alpha_2 - \gamma_2 \mathcal{Y}_t)dt + \sigma_2 dW_t^2$$
$$dW_t^1 dW_t^2 = \rho dt$$

where S_t is the spot price or spread; q_t is the deterministic function; $\mathcal{X}_t$ is the short term deviation and $\mathcal{Y}_t$ is the long term equilibrium level

◆ This model leads to a closed form solution of forward prices and thus forward term structure.

Risk Neutral Simulation: Volatility

◆ In the risk neutral world, the volatility is embedded in the price simulation.

◆ Thus, there is no need to simulate implied volatilities.

Credit Exposure Approach Implementation

◆ Obtain the risk-free value $V_f(t)$ of a counterparty portfolio that should be reported by trading systems.

◆ The solution is based on the existing credit exposure framework.

◆ Switch simulation from the real-world measure to the risk neutral measure.

◆ Calculate discounted risk-neutral credit exposures (EEs) and take master agreement and CSA into account.

◆ One can directly compute CVA using the following formula

$$CVA = (1 - R) \sum_{k=1}^{N} [PD(t_k) - PD(t_{k-1})] EE^*(t)$$

Credit Exposure Approach Implementation (Cont'd)

◆ Or one can compute the risky value $V_r(t)$ of the portfolio via discounting positive EEs by counterparty's CDS spread + risk-free interest rate as the positive EEs bearing counterparty risk and negative EEs by the bank's own CDS spread + risk-free interest rate as the negative EEs bearing the bank's credit risk.

$$CVA = V_f(t) - V_r(t)$$

◆ Furthermore, you can compute the funding value $V_F(t)$ of the portfolio via discounting positive EEs by counterparty's bond spread + risk-free interest rate and negative EEs by the bank's own bond spread + risk-free interest rate.

$$FVA = V_f(t) - V_F(t) - CVA = V_r - V_F$$

Least Square Monte Carlo Approach Implementation

◆ Obtain the risk-free value $V_f(t)$ of a counterparty portfolio that should be reported by trading systems.

◆ Simulate market risk factors in the risk-neutral measure.

◆ Generate payoffs for all trades based on Monte Carlo simulation.

◆ Aggregate payoffs based on the Master agreement and CSA.

◆ Compute the risky value $V_r(t)$ of the portfolio using Longstaff-Schwartz approach.

LSMC Approach Implementation (Cont'd)

◆ Positive cash flows should be discounted by counterparty's CDS spread + risk-free interest rate while negative cash flows should be discounted by the bank's own CDS spread + risk-free interest rate.

◆ $CVA = V_f(t) - V_r(t)$

◆ Moreover, you can compute the funding value $V_F(t)$ of the portfolio using Longstaff-Schwartz approach as well

◆ Positive cash flows should be discounted by counterparty's bond spread + risk-free interest rate while negative cash flows should be discounted by the bank's own bond spread + risk-free interest rate.

◆ $FVA = V_f(t) - V_F(t) - CVA = V_r - V_F$

Reference:
https://finpricing.com/lib/EqWarrant.html